### NASA/TM-2008-215430



# Shear Modulus for Nonisotropic, Open-Celled Foams Using a General Elongated Kelvin Foam Model

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#### Summary

An equation for the shear modulus for nonisotropic, open-celled foams in the plane transverse to the elongation (rise) direction is derived using an elongated Kelvin foam model with the most general geometric description. The shear modulus was found to be a function of the unit cell dimensions, the solid material properties, and the cell edge cross-section properties. The shear modulus equation reduces to the relation derived by others for isotropic foams when the unit cell is equiaxed.

#### Introduction

Over the years, there have been numerous attempts to develop equations that are capable of predicting the strength and the elastic properties of open- and closed-cell foams from a description of the foam microstructure and a measure of the cell dimensions. This endeavor requires selecting a suitable representative element to mimic the foam microstructure. Many of these micromechanics models have used a tetrakaidecahedron (a 14-sided polyhedron) to represent the foam microstructure. This choice follows from the work of Thomson (1887) who argued that the 14-sided polyhedron (with slightly curved faces) was the naturally preferred shape for soap bubbles and other foams as it is the shape that minimizes the surface area per unit volume and still packs to fill space. As a result, the tetrakaidecahedron model is widely known as the Kelvin foam model.

Some of the more notable studies in this area are the works of Zhu, Knott, and Mills (1997), Warren and Kraynik (1997), Dement'ev and Tarakanov (1970), and Gong, Kyriakides, and Jang (2005). Zhu used an equiaxed tetrakaidecahedron and assumed that the behavior of open-celled foams could be simulated by treating the cell edges as structural elements possessing axial, bending, and torsional rigidity. They applied the minimum potential energy theorem to the unit cell deformation and developed equations for the Young's modulus, the shear modulus, and Poisson's ratio for isotropic, open-celled foams. These equations were derived in terms of the cell edge lengths, the edge cross-section properties, and the solid material properties.

In some cases, the foam cells are elongated; as a result, these foams exhibit a nonisotropic mechanical behavior. Such is the case in spray-on foams where the cells become elongated in the rise direction during the foaming and rising process. To treat nonisotropic, open-celled foams, Dement'ev and Tarakanov (1970) used an elongated Kelvin model to derive equations for the elastic constants and compressive strengths in the principal material directions. The equations for the elastic constants were derived by considering the flexural deformation of the cell edges under the applied stresses. The compressive strength equations were obtained based on the critical (Euler) buckling load of the edges.

Gong, Kyriakides, and Jang (2005) also adopted an elongated Kelvin unit cell to model nonisotropic foams. They improved upon the fidelity of the previous models by using Plateau borders to represent the edge cross sections and by allowing the dimensions of the cross section to vary along the edge length. They also included the effects of shear deformation.

The size and shape of the elongated Kelvin unit cell used by Dement'ev and Tarakanov (1970), Gong, Kyriakides, and Jang (2005), and others are defined by specifying two unit cell dimensions: either the cell height and cell width or the height-to-width ratio and one of the two cell dimensions. In the most general sense, however, an elongated tetrakaidecahedron has three independent dimensions. Sullivan, Ghosn, and Lerch (2008) recognized this shortcoming with the previous models and proposed using an elongated Kelvin model with three independent dimensions to model nonisotropic, open-celled foams. Following the same approach as Zhu, Knott, and Mills (1997), Sullivan, Ghosn, and Lerch (2008) applied the principle of minimum potential energy to the unit cell deformation and derived the equations for the Young's modulus, Poisson's ratios, and tensile strengths in the principal material directions, thereby establishing a foam micromechanics model using the most general Kelvin unit cell.

This report is intended as a supplement to Sullivan, Ghosn, and Lerch (2008) as it uses the general Kelvin unit cell model and a similar potential energy approach to develop the equation for the shear modulus in the plane perpendicular to the elongated (rise) direction. Herein, the general Kelvin foam model is reviewed. Since the elongated Kelvin unit cell is symmetric, one-quarter of the Kelvin cell is chosen as the repeating unit cell. Displacement conditions are applied to the unit cell boundaries to ensure that the unit cell remains a representative repeating unit during shear deformation. The principle of minimum potential energy is applied to the unit cell deformation, yielding an algebraic equation for the shear strain in terms of the shear stress. From this, the equation for the shear modulus is derived.

#### **Elongated Kelvin Unit Cell**

The general elongated tetrakaidecahedron (Kelvin foam model) is a 14-sided polyhedron constructed from 8 hexagonal faces, 4 vertical rhombic faces, and 2 horizontal square faces (fig. 1). The vertical rhombic faces have sides of length L, and the horizontal square faces have sides of length b. The hexagonal faces have four sides of length L and two sides of length L. The inclination angle  $\theta$  defines the orientation of the hexagonal faces with respect to the rise direction as well as the obtuse angle of the vertical diamond faces  $2\theta$ . The edges are the line segments formed by the intersection of multiple faces. Thus, the edges will be of length L or b.

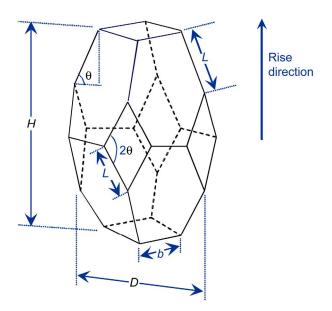


Figure 1.—Elongated tetrakaidecahedron repeating unit cell (Kelvin model).

Since the cell height H and cell width D are related to the edge lengths L and b and the inclination angle  $\theta$  according to

$$H = 4L\sin\theta$$
 and  $D = 2L\cos\theta + \sqrt{2}b$  (1)

the size and shape of the general elongated tetrakaidecahedron are defined by specifying three of the five unit cell dimensions shown in figure 1.

In open-celled foams, all the solid mass is concentrated within the cell edges. The edges are assumed to behave like structural members, possessing axial, flexural, and torsional rigidity. They have cross-sectional area A, bending moment of inertia I, and torsion constant J. The Young's modulus of the solid material is denoted as E and the shear modulus as G.

#### **Unit Cell Deformation**

We first establish a Cartesian coordinate system XYZ such that the Z-axis is oriented in the elongation or rise direction (fig. 2). The X-axis is parallel to a line normal to two of the vertical rhombic faces, and the Y-axis is parallel to a line normal to the other two vertical rhombic faces. We seek to derive the equation for the foam shear modulus  $G_{xy}$ . For this purpose, we adopt the structural unit shown in red in figure 2 as the representative repeating unit. This repeating unit is a one-quarter segment of the Kelvin foam unit cell shown in figure 1.

Next, we establish the  $X_sY_sZ$ -coordinate system that is oriented with respect to the XYZ-system by a 45° counterclockwise rotation about the Z-axis. The repeating structural unit is bounded by six symmetry planes: two planes parallel to the  $Y_sZ$ -plane, two planes parallel to the  $X_sZ$ -plane, and two planes parallel to the  $X_sY_s$ -plane. Since the members AN, AO, BJ, BK, DM, DL, EP, and EQ all lie within the  $X_sY_s$ -symmetry planes, they are shared by two adjacent unit cells. As such, we assume that within the unit cell, they possess a cross-sectional area A/2 and a bending moment of inertia I/2. The repeating structural unit and symmetry planes constitute the repeating unit cell for determining the shear modulus  $G_{xy}$ .

The normal stresses  $\tau$  and  $-\tau$  are applied in the  $X_s$ - and  $Y_s$ -directions, respectively, as shown in figure 3. We define the displacements of the unit cell with respect to the unit cell center at point C and assume that all displacements and rotations at point C are zero. The applied loading results in a unit cell displacement of 2u in the  $X_s$ -direction and -2u in the  $Y_s$ -direction, where both displacements are symmetric about point C. There is no displacement of the unit cell in the Z-direction (fig. 4).

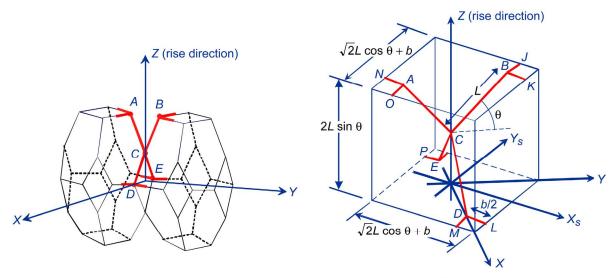


Figure 2.—One-quarter model showing its reference with respect to elongated Kelvin unit cell (point Q not shown; see figs. 3 and 4).

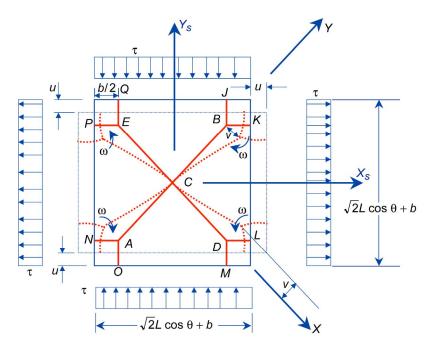


Figure 3.—Applied loading and deformed shape of unit cell (XY-plane).

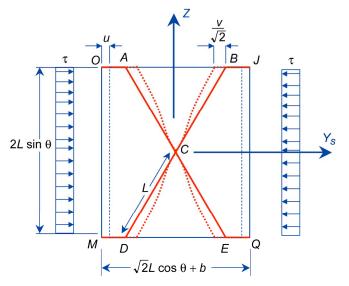


Figure 4.—Applied loading and deformed shape of unit cell  $(Y_sZ$ -plane).

In the deformed structure, we assume that the symmetry planes remain orthogonal. Any edge that is initially normal to a symmetry plane boundary will remain normal to it after the deformation. Thus, the points J, K, L, M, N, O, P, and Q do not rotate during the deformation. Furthermore, the half-edges AN, AO, BJ, BK, DL, DM, EQ, and EP must remain in their respective symmetry planes. Thus, the points A, B, D, and E translate within their respective symmetry planes and the only rotation of these points is about the E-axis. Point E translates in the E-direction by an amount E0 and E1 translates by an amount E2 and E3 undergo a clockwise rotation E3 about the E3-axis, and points E4 and E5 undergo a counterclockwise rotation E6.

We note that as a result of similarity and symmetry, the deformed shape and the deformation energy of member BC are the same as those of members CD, AC, and CE. Likewise, the deformed shape and

deformation energy of the members BK, DL, AN, and EP are equivalent and those of members BJ, DM, AO, and EQ are equivalent. Furthermore, the axial tension in member BK is equal to the axial compression in member BJ, and the bending moment in BJ is equal to the bending moment in BK. Thus, the deformation energy of the entire unit cell can be determined from the strain energy of deformation of only members BC and BK.

## Strain Energy of Member BC

We will make use of a third coordinate system X'Y'Z', where the Y'-axis is oriented along the length of member BC as shown in figure 5. Since there is no normal stress applied to the unit cell in the Y- or Z-direction (see fig. 3), the axial force  $N_{BC}$ , the shear force  $V_z$ , as well as the bending moment about the X'-axis  $M_{x'}$ , must be zero throughout the length of the member. Furthermore, there is no deformation of member BC in the YZ- (or Y'Z'-) plane. The only deformation energy in member BC is that associated with bending about the Z'-axis  $M_{z'}^{BC}$  and the torsional deformation associated with  $M_{y'}^{BC}$ . The displacements and rotations at point B in the X'YZ'-coordinate system are summarized as

The member end forces and moments at point B are shown in figure S(a), and the active degrees of freedom at B are shown in figure S(b).

Considering the deformation of member BC in the X'Y'-plane, the member end displacement and rotation at point B are related to the member end force and moment (fig. 6), using the first and second moment-area theorems as

$$\frac{M_{z'}^{BC}L}{EI} + \frac{V_x^B L^2}{2EI} = \omega \cos \theta \tag{2}$$

and

$$\frac{M_{z'}^{BC}L^2}{2EI} + \frac{V_x^B L^3}{3EI} = v \tag{3}$$

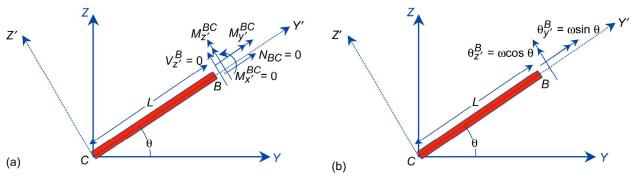


Figure 5.—Member *BC* showing member end forces and moments and member end displacements and rotations at point *B* in *YZ*-plane. (a) End forces and end moments. (b) End displacements and rotations.

respectively. Solving equations (2) and (3) simultaneously, we obtain

$$V_x^B = \frac{12EI}{L^3} \left( v - \frac{\omega L}{2} \cos \theta \right) \tag{4}$$

$$M_{z'}^{BC} = \frac{2EI}{L} \left( 2\omega \cos \theta - 3\frac{v}{L} \right) \tag{5}$$

Considering the torsional deformation of member BC yields

$$M_{y'}^{BC} = \frac{GJ}{L} \omega \sin \theta \tag{6}$$

The strain energy for member BC is

$$U_{BC} = \frac{\left(M_{y'}^{BC}\right)^{2} L}{2GJ} + \frac{1}{2EI} \int_{0}^{L} \left(M_{z'}^{BC} + V_{x}^{B} s\right)^{2} ds$$

where s is the local coordinate oriented along member BC, having the value s = 0 at point B and s = L at point C. Using equations (4), (5), and (6), the strain energy may be written in terms of the displacements v and  $\omega$  as

$$U_{BC} = \frac{GJ}{2L}\omega^2 \sin^2\theta + \frac{EI}{L^3} \left( 2L^2\omega^2 \cos^2\theta + 6v^2 - 6vL\omega\cos\theta \right)$$
 (7)

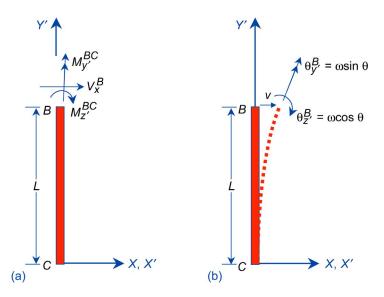


Figure 6.—Member *BC* showing member end forces and moments and member end displacements and rotations in *X'Y'*-plane. (a) End forces and moments. (b) End displacements and rotations.

# Strain Energy of Member BK

Member BK remains in the symmetry plane defined by the points A, B, and K. The only deformation energy in member BK is that associated with the axial extension and bending about the Z-axis. There is no  $Y_s$ -direction loading on member BK at point K. Thus, there is no transverse (shear) force in the member, and the bending moment about the Z-axis is constant along the member length. Transforming the displacements at point B into the  $X_sY_sZ$ -coordinate system, we have  $u_{x_s}^B = v/\sqrt{2}$ ,  $u_{y_s}^B = -v/\sqrt{2}$ ,  $u_z^B = 0$ . The member end forces and moments in member BK are shown in figure T(a), and the member end point displacements and rotations are shown in figure T(b).

The equation for the axial extension of member BK is

$$u - \frac{v}{\sqrt{2}} = \frac{N_{BK} \left(\frac{b}{2}\right)}{E\left(\frac{A}{2}\right)}$$

The end point rotations may be written in terms of the bending moment  $M_z$  by the first moment-area theorem as

$$\theta_z^B - \theta_z^K = \omega - 0 = \frac{M_z^{BK} \left(\frac{b}{2}\right)}{E\left(\frac{I}{2}\right)}$$

Rewriting the previous two equations, we obtain

$$N_{BK} = \frac{EA}{b} \left( u - \frac{v}{\sqrt{2}} \right) \tag{8}$$

$$M_z^{BK} = \frac{EI}{b}\omega \tag{9}$$

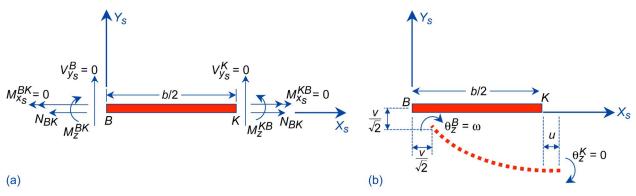


Figure 7.—Member *BK* showing member end forces and moments and member end displacements and rotations. (a) End forces and moments. (b) End displacements and rotations.

The strain energy for member BK is

$$U_{BK} = \frac{N_{BK}^{2} \left(\frac{b}{2}\right)}{2\left(\frac{A}{2}\right)E} + \frac{1}{2E\left(\frac{I}{2}\right)} \int_{0}^{b/2} \left(M_{z}^{BK}\right)^{2} ds$$

which, by substituting equations (8) and (9), may be written in terms of the displacements u, v, and  $\omega$  as

$$U_{BK} = \frac{EA}{2b} \left( u - \frac{v}{\sqrt{2}} \right)^2 + EI \frac{\omega^2}{2b} \tag{10}$$

#### **Derivation of Shear Modulus Equation**

As a result of the symmetry and similarity of the unit cell deformation, the strain energy for the repeating unit cell shown in figure 2 is

$$U = 4U_{BC} + 8U_{BK} \tag{11}$$

The work done on the unit cell by the applied loading is

$$W = 8L\sin\theta \left(\sqrt{2}L\cos\theta + b\right)\tau u \tag{12}$$

Substituting equations (7) and (10) into (11) and applying the minimum potential energy theorem

$$\frac{\partial(W-U)}{\partial u} = 0 \qquad \frac{\partial(W-U)}{\partial v} = 0 \qquad \frac{\partial(W-U)}{\partial \omega} = 0$$

lead to

$$\frac{2EA}{b}u - \sqrt{2}\frac{EA}{b}v = 2L\sin\theta\left(\sqrt{2}L\cos\theta + b\right)\tau\tag{13a}$$

$$-\sqrt{2}\frac{EA}{b}u + \left(\frac{12EI}{L^3} + \frac{EA}{b}\right)v - \frac{6EI}{L^2}\cos\theta\omega = 0$$
 (13b)

$$-\frac{6EI}{L^2}\cos\theta v + \left(\frac{2EI}{b} + \frac{GJ}{L}\sin^2\theta + \frac{4EI}{L}\cos^2\theta\right)\omega = 0$$
 (13c)

Solving equations (13) simultaneously yields

$$u = \tau L \sin \theta \left( \sqrt{2}L \cos \theta + b \right) \left( \frac{b}{EA} + \frac{L^3 \left( 2L + 4b \cos^2 \theta + \frac{GJ}{EI} b \sin^2 \theta \right)}{12EI \left( 2L + b \cos^2 \theta + \frac{GJ}{EI} b \sin^2 \theta \right)} \right)$$
(14a)

$$v = \tau L^4 \sin \theta \left( \sqrt{2}L \cos \theta + b \right) \left( \frac{2L + 4b \cos^2 \theta + \frac{GJ}{EI} b \sin^2 \theta}{6\sqrt{2}EI \left( 2L + b \cos^2 \theta + \frac{GJ}{EI} b \sin^2 \theta \right)} \right)$$
(14b)

$$\omega = \tau bL^{3} \sin \theta \cos \theta \left( \sqrt{2}L \cos \theta + b \right) \left( \frac{1}{\sqrt{2}EI \left( 2L + b \cos^{2} \theta + \frac{GJ}{EI}b \sin^{2} \theta \right)} \right)$$
(14c)

The principal strains are  $2u/(\sqrt{2}L\cos\theta + b)$  and  $-2u/(\sqrt{2}L\cos\theta + b)$ , so the shear strain is  $\gamma = 4u/(\sqrt{2}L\cos\theta + b)$ . Since  $\tau = G_{xy}\gamma$ , then

$$\frac{1}{G_{xy}} = \frac{4u}{\tau \left(\sqrt{2}L\cos\theta + b\right)} = 4L\sin\theta \left\{ \frac{b}{EA} + \frac{L^3 \left[EI\left(2L + 4b\cos^2\theta\right) + GJb\sin^2\theta\right]}{12EI\left[EI\left(2L + b\cos^2\theta\right) + GJb\sin^2\theta\right]} \right\}$$
(15)

Rearranging equation (15), we obtain finally

$$G_{xy} = \frac{12EAI\left(2L + b\cos^2\theta + \frac{GJ}{EI}b\sin^2\theta\right)}{H\left[12Ib\left(2L + b\cos^2\theta + \frac{GJ}{EI}b\sin^2\theta\right) + AL^3\left(2L + 4b\cos^2\theta + \frac{GJ}{EI}b\sin^2\theta\right)\right]}$$

Note that when b = L and  $\theta = \pi/4$ , the expression for the shear compliance  $G_{xy}^{-1}$  reduces to

$$\frac{1}{G_{xv}} = \frac{2\sqrt{2}L^2}{EA} + \frac{\sqrt{2}L^4}{6EI} \left(\frac{8EI + GJ}{5EI + GJ}\right)$$

which is the expression obtained by Zhu, Knott, and Mills (1997) for isotropic foams.

# **Concluding Remarks**

The equation for the shear modulus for nonisotropic, open-celled foams in the plane transverse to the elongation (rise) direction was derived. The equation was derived using an elongated Kelvin foam model with the most general geometric description, one that requires specifying three unit cell dimensions to define its size and shape. The shear modulus is a function of the unit cell dimensions, the solid material Young's modulus E and shear modulus E, and the edge cross-section properties E, E, and E. It can be shown that the shear modulus equation derived from the most general elongated Kelvin unit cell shape reduces to the relation derived by Zhu, Knott, and Mills (1997) for isotropic foams when the unit cell is equiaxed.

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